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| 科目名稱 | 材料力學 | 類組代碼 | D37 |
| | | 科目碼 | D3793 |

※本項考試依簡章規定所有考科均「不可」使用計算機。

本科試題共計 2 頁

1. A stepped bar ACB with square cross sections is held between rigid supports and loaded by an axial force P at midlength (see Figure 1). The width for the two parts of the bar are $b_1 = d_1 = 20$ mm and $b_2 = d_2 = 40$ mm, and the material is elastoplastic with yield stress $\sigma_y = 250$ MPa. Determine the plastic load P_p . (20%)

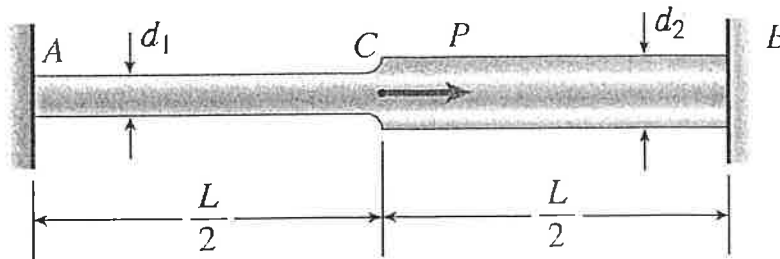


Figure 1

2. A simple beam AB shown in Figure 2 is subjected to a distributed load of intensity $q(x) = q_0 \sin \frac{\pi x}{L}$, where q_0 is the maximum intensity of the load. Determine the maximum absolute value of the bending moment M_{\max} , and the maximum deflection δ_{\max} in the beam. (20%)

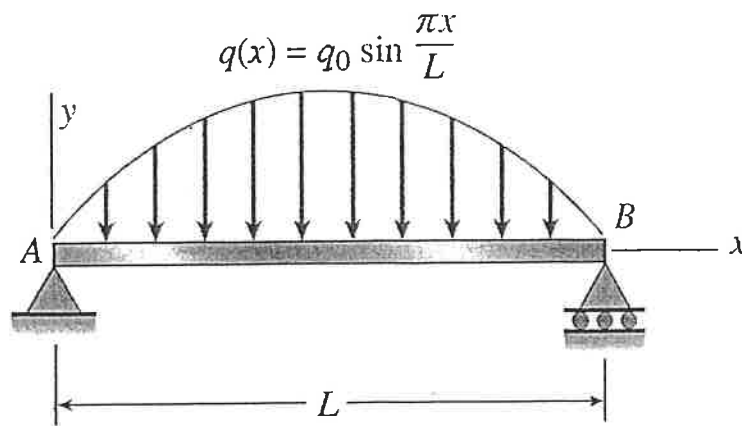


Figure 2

3. In Figure 3, a cantilever beam of length L and loaded by uniform load of intensity q has a fixed support at A and spring support at B with rotational stiffness k_R . A rotation at B , θ_B , results in a reaction moment $M_B = k_R \times \theta_B$. Use the second-order differential equation of the deflection curve to solve for displacements δ_B at end B . (20%)

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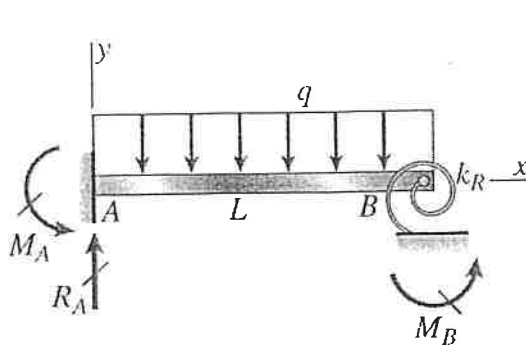


Figure 3

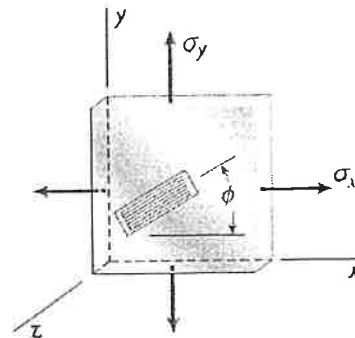
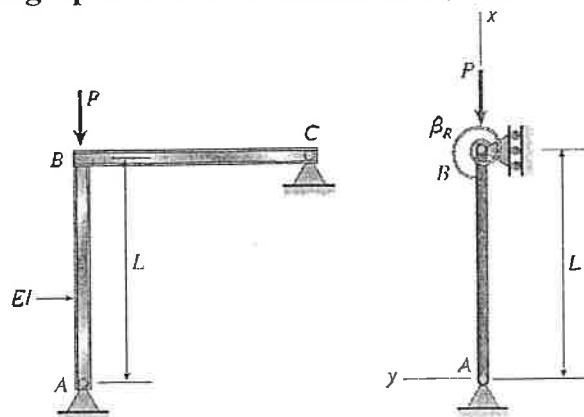


Figure 4

- A steel plate with a modulus of elasticity $E = 200 \text{ GPa}$ and Poisson's ratio $\nu = 0.3$ is loaded in biaxial stress by normal stresses σ_x and σ_y (see Figure 4). A strain gage is bonded to the plate at an angle $\phi = 30^\circ$. If the stress σ_x is 100 MPa and the strain measured by the gage is $\varepsilon = 340 \times 10^{-6}$, what is the **maximum in-plane shear stress** $(\tau_{\max})_{xy}$ and **maximum in-plane shear strain** $(\gamma_{\max})_{xy}$? (20%)
- The frame ABC consists of two members AB and BC that are rigidly connected at joint B , as shown in part (a) of the Figure 5. The frame has pin supports at A and C . A concentrated load P acts at joint B , thereby placing member AB in direct compression. To assist in determining the buckling load for member AB , represent it as a pinned-end column, as shown in part (b) of the Figure 5. At the top of the column, a rotational spring of stiffness β_R represents the restraining action of the horizontal beam BC on the column (note that the horizontal beam provides resistance to rotation of joint B when the column buckles). Also, consider only bending effects in the analysis (i.e., disregard the effects of axial deformations). By solving the differential equation of the deflection curve, derive the **buckling equation** for this column AB . (20%)



(a)

(b)

Figure 5