## 臺灣綜合大學系統112學年度學士班轉學生聯合招生考試試題

科目名稱	微積分C	類組代碼	共同考科
		科目碼	E0013
		本科試題共計 1 頁	

1. (10 points) Evaluate the limit

$$\lim_{x \to 1} \frac{\sqrt{x} - 1}{x - 1}.$$

2. (10 points) Evaluate

$$\int_0^{\frac{\pi}{2}} \sin^2 x \cos x \, dx.$$

3. (10 points) Evaluate

$$\int_0^1 \frac{1}{x^2 + 2} \, dx.$$

4. (10 points) Find the arc length of the cycloid

$$C: \begin{cases} x = r(\theta - \sin \theta) \\ y = r(1 - \cos \theta) \end{cases}, \quad 0 \le \theta \le \frac{\pi}{2}.$$

- 5. (10 points) Find the 5th derivative  $f^{(5)}(0)$  of the function  $f(x) = \ln(1+x) \cdot \tan^{-1} x$ .
- 6. (10 points) Find the maximum value of the function f(x, y, z) = x + 2y + 3z on the curve of intersection of the plane x y + z = 0 and the cylinder  $x^2 + y^2 = 29$ .
- 7. (10 points) Find the surface area of the part of the paraboloid  $z = x^2 + y^2$  that lies between the planes z = 1 and z = 9.
- 8. (10 points) Evaluate

$$\iiint_{R} e^{(x^2+y^2+z^2)^{\frac{3}{2}}} dV,$$

where  $B = \{(x, y, z) \mid x^2 + y^2 + z^2 \le 1\}$  is the unit ball.

9. (10 points) Evaluate

$$\oint_C (y^2 + \sin x) dx + (3xy - e^y) dy$$

where C is the boundary of the semiannular region D in the upper half-plane between the circles  $x^2 + y^2 = 4$  and  $x^2 + y^2 = 9$ .

10. (10 points) Evaluate  $\iint_S \mathbf{F} \cdot d\mathbf{S}$ , where

$$\mathbf{F}(x,y,z) = xy\,\mathbf{i} + (y^2 + e^{xz})\,\mathbf{j} + \cos(xy)\,\mathbf{k}$$

and S is the surface of the region E bounded by the parabolic cylinder  $z = 1 - x^2$  and the planes z = 0, y = 0, y + z = 2.